# Program for the Indiana Section MAA Fall Meeting 2017 Manchester University, North Manchester Saturday, October 7, 2017 Science Center (SCIC) 604 E College Ave, North Manchester IN 46962

8:00am-9:00am	Registration & Breakfast Refreshments		
SCIC Atrium	Refreshments provided by the Dean of Natural and Health Sciences		
8:00am-3:00pm	MAA book kiosk: computer to order MAA books at discount;		
SCIC 103	New MAA books to browse during contributed talks		
8:25am-8:40am	Welcome		
Flory Auditorium	Tim Brauch, Chair of Department of Mathematics and Computer Science, Manchester University		
SCIC 203	Mark Huntington, Dean of Natural and Health Sciences, Manchester University		
SCIC 203	Dave McFadden, President, Manchester University		
8:40am-9:30am	Some Unusual Applications of Mathematics		
Flory Auditorium	Ron Gould, Department of Mathematics		
SCIC 203	Emory University		
9:30am-9:40am	Coffee Break		
SCIC Atrium	Conee Break		
9:40am-10:30am	Challenges of Researching Integer Sequences Using the OEIS		
Flory Auditorium	Gene Fiorini, Department of Mathematics		
SCIC 203	Muhlenberg College		

	Contributed Talks							
Room	SCIC 101	SCIC 104	SCIC 202	SCIC 203	SCIC 204			
10:45am- 11:10am	Results on Regular and Nearly Regular VE- and EV-Degree Sequences	Global Dynamics of the Shadow Gierer- Meinhardt System with Mixed Boundary Conditions	Solutions of the Nonlinear Polyharmonic Equation with Periodic Potential		Ethical Considerations in the Era of Big Data			
	Ryan Morley**  Manchester University	Kwadwo Antwi- Fordjour Earlham College	Seonguk Kim DePauw University		Stacy Hoehn Franklin College			
11:20am- 11:45am	Serious Math for Playful Young Minds	Multilinear Algebra and its Applications	Aero Cube S4 Group Theory Blocks	Implementing the 2015 CUPM Content Recommendations	Exceptional Elliptic Curves with Specified Torsion Subgroups			
	Shwan Ma Pi Math Learning Center	Anmol Lamichhane** Earlham College	Dennis G. Collins UPR-Mayaguez	IN-NExT Panel:	Alexander J. Barrios*  Purdue University			
11:55am 12:20pm	Set Problems Involving Symmetric Difference	Refuting a Conjecture On $x^n - 1$ Using a Computer Algebra System	Addressing Conservative Issues Associated with Adaptive Simulations	Paul Fonstad Franklin College Lara Pudwell Valparaiso University Moderator: Livia				
	Rodney Lynch <i>IUPUC</i>	Michael Xue Vroom Laboratory for Advanced Computing	Godfred Yamoah Trine University	Hummel University of Indianapolis				

Student Talks: (\*) Graduate Student; (\*\*) Undergraduate Student
\*\*Each talk is to be a 20 minute talk followed by 5 minutes for questions\*\*

12:30pm-1:30pm	Lunch		
SCIC Atrium	Additional lunch seating is available in SCIC 204		
12:30pm-1:30pm	Executive Board Committee Meeting		
SCIC 202	Executive Board Commuteet Meeting		
1:35pm-2:25pm	Math and Marriage - Don't Call a Lawyer Yet		
Flory Auditorium	Ron Gould, Department of Mathematics		
SCIC 203	Emory University		
2:30pm-2:45pm	Coffee Break		
SCIC Atrium			
2:45pm-3:45pm	Proposal Writing Workshop		
Flory Auditorium	Gene Fiorini, Department of Mathematics		
SCIC 203	Muhlenberg College		

GENERAL ADJOURNMENT

# **Abstracts for Talks**

An alphabetical listing of authors appears at the end. 8:40am-9:30am

• Some Unusual Applications of Mathematics, Ron Gould, Department of Mathematics, *Emory University* (SCIC 203) In math classes we often see applications of mathematics to other areas such as physics, chemistry, biology, economics and more. But mathematics has applications in many places we might not expect. This talk will show you a variety of fairly simple applications of basic mathematics to more unusual problems, puzzles and games.

# 9:40am-10:30am

• Challenges of Researching Integer Sequences Using the OEIS, Gene Fiorini, Department of Mathematics, *Muhlenberg College* (SCIC 203)

Sequences play an important role in number theory, combinatorics and discrete mathematics, among many other fields. They enumerate objects in sets and define relationships among items or properties shared between them. Integer sequences have inspired mathematicians for centuries. Likewise, they also inspire computer scientists. The quest to compute new, larger terms in important infinite sequences is harnessing the power of computing and promoting the use of new paradigms in distributed and cloud computing as well as Big Data. Current examples include the "Great Internet Mersenne Prime Search" to find Mersenne primes (sequence A000668 in OEIS) and Microsoft's challenge to discover non-Mersenne or "lost" primes (sequence A138837). By gathering sequences – and a wealth of information about them – together in a common database, the OEIS (Online Encyclopedia of Integer Sequences), established by Neil Sloane, provides the mathematically curious an invaluable resource with which to explore. This talk presents some interesting sequences found in the OEIS along with its role in stimulating new research.

#### 10:45am-11:10am

Results on Regular and Nearly Regular VE- and EV-Degree Sequences, Ryan Morley\*\*, Manchester University (SCIC 101)

We will start this talk with a brief introduction to graph theory followed by definitions and examples of VE-degrees and degree sequences. We present some classic results for degree sequences, such as Havel –Hakimi and show our results identifying graphical ve-degree sequences for complete, nearly complete, and bipartite graphs. We finish the talk by giving definitions, examples, and results for ev-degrees and degree sequences. This work was supported by a Faculty-Student Summer Research Grant under the guidance of Dr. Timothy M. Brauch, Manchester University

• Global Dynamics of the Shadow Gierer-Meinhardt System with Mixed Boundary Conditions, Kwadwo Antwi-Fordjour, *Earlham College*, (SCIC 104)

One of the famous models studied in biological pattern formation is the Gierer-Meinhardt system based on Turing's idea. This system can be used to model skeletal limb development in humans under certain boundary conditions. In this talk, the global dynamics of the shadow Gierer-Meinhardt system will be considered with Robin boundary conditions on one concentration and Neumann boundary conditions on the other.

• Solutions of the Nonlinear Polyharmonic Equation with Periodic Potential, Seonguk Kim, *DePauw University* (SCIC 202)

In this talk, we investigate quasi-periodic solutions of a nonlinear periodic polyharmonic equation, which is relevant to the study of a Bose-Einstein condensate loaded into optical lattices. In the first part of this study, we consider the perturbation formulas for a linear operator with periodic potential. To do so, I will introduce simple properties: spectral projection and matrix representation, from linear algebra and complex analysis courses. Second, we use the results for the linear equation to find quasi-periodic solutions for the nonlinear periodic polyharmonic equation.

Ethical Considerations in the Era of Big Data, Stacy Hoehn, Franklin College (SCIC 204)

Every time we log on to social media, view a website, use a credit card, or use a loyalty rewards card, someone somewhere is gathering data about us. More and more companies and organizations are turning to big data to better find customers and tailor their marketing to them. Yet for every benign use of big data, there also are ones that are unintentionally discriminatory or, worse, intentionally predatory. Since the use of big data is going to continue to grow, it is important to not only help our students learn how to analyze data but also to make our students aware of possible negative consequences of using data to make decisions that affect people's lives. This talk will provide some suggestions for how to incorporate discussions of the ethics of big data in a variety of undergraduate courses

#### 11:20am-11:45am

- Serious Math for Playful Young Minds, Shwan Ma, *Pi Math Learning Center* (SCIC 101)

  How to make STEM relevant to young learners age 8 -15? Is a middle schooler too young to learn Data science, Encryption, Optimization? How to apply foundational math topics to the emerging studies of tomorrow? This talk presents a math enrichment program of Central Indiana (Pi Math) a part of MAA Math Circle SIG and MISR's outreach program, aiming at getting children excited about mathematics. Through hands-on games and puzzles, this talk illustrates how students learn in a collaborative environment the skills of critical thinking, problem solving and logic reasoning
- Multilinear Algebra and its Applications, Anmol Lamichhane\*\*, Earlham College (SCIC 104) "What is a vector? What does it represent physically?" We will start with the question and then attempt to answer that by using the idea of vector space. We will then extend the notion of linear maps to define multi-linear maps and present an example from physics where one uses the multi-linearity property of tensors to "shrink" a complicated-looking expression into a simpler one.
- Aero Cube S4 Group Theory Blocks, Dennis G. Collins, *UPR-Mayaguez* (SCIC 202)

  This talk presents a set of blocks that compute the rotation group of a cube, which is isomorphic to the symmetry group S4 of order 24. This set may be termed "verb blocks" and follows up on a talk "Math Magic Number Blocks and the Wobble Square Method of Multiplication" presented Oct. 18, 2014 at the MAA Indiana Section Meeting at Trine University and Aug. 5, 2015 at the MAA Mathfest in Washington, D.C., covering what may be termed "noun blocks." The said verb blocks show the equivalence of four major methods of group calculation in this case, namely 1) aero manipulations, 2) group cycle calculation, 3) matrix multiplication, and 4) quaternion multiplication. The blocks can operate either on themselves or on the number blocks and might be termed "religious tolerance blocks" since any of the rather different methods of calculation leads to the same result. There seems to be some kind of "twist" involved in all the methods. However the blocks, based on 90 degree rotations, apparently do not extend to, say, 45 degree rotations as a closed set. Conversations with Glenn Collins are acknowledged.
- Exceptional Elliptic Curves with Specified Torsion Subgroups, Alexander J. Barrios\*, Purdue University (SCIC 204) The *ABC* conjecture of Masser and Oesterlé proposed in 1985 states that for each  $\epsilon > 0$  there are only finitely many relatively prime positive integers A, B, C with A + B = C and  $\operatorname{rad}(ABC)^{1+\epsilon}$  where  $\operatorname{rad}(a)$  denotes the product over all the distinct prime factors of a. If  $\epsilon = 0$ , it is well known that there are infinitely many triples of integers as above satisfying the inequality. The *ABC* conjecture is equivalent to the modified Szpiro conjecture which states that for each  $\epsilon > 0$  there are only finitely many rational elliptic curves E such that  $N_E^{6+\epsilon} < \max\{|c_4|^3, |c_6|^2\}$  where  $c_4$  and  $c_6$  are the invariants associated to a minimal model of E, and  $N_E$  denotes the conductor of E. A rational elliptic curve is said to be exceptional if it satisfies the above inequality with  $\epsilon = 0$ . By Mazur's Theorem there are only fifteen possible groups T such that  $E(\mathbb{Q})_{tors} \cong T$ . We prove that for each T, there are infinitely many exceptional elliptic curves E with  $E(\mathbb{Q})_{tors} \cong T$ .

# 11:20am-12:20pm

- Implementing the 2015 CUPM Content Recommendations, IN-NExT Panel:, Paul Fonstad, Franklin College, Lara Pudwell, Valparaiso University, Moderator: Livia Hummel, University of Indianapolis (SCIC 203)

  The 2015 CUPM Content Recommendations include elements common across degree programs in the mathematical sciences. The panelists will share their institutional perspectives and experiences regarding implementation of these content recommendations. In particular, they will comment on their experiences with the following recommendations:
  - Content Recommendation #3: Mathematical sciences major programs should include concepts and methods from data analysis, computing, and mathematical modeling.
  - o Content Recommendation #5: All students majoring in the mathematical sciences should experience mathematics from the perspective of another discipline.

However, these perspectives should be viewed only as a starting point for conversation. Thus, this session will encourage discussion and perspectives from attendees regarding the challenges of and successes in implementation in a variety of institutional settings.

### 11:55am-12:20pm

• **Set Problems Involving Symmetric Difference**, Rodney Lynch, IUPUC (SCIC 101) Recall the symmetric difference of two sets A and B is given by  $A \triangle B = (A \setminus B) \cup (B \setminus A)$ . Can you find three sets A, B, and C which satisfy:  $A \triangle B \triangle C = \{2, 3, 4\}$ ,  $B \triangle C = \{1, 3, 5\}$ ,  $A \triangle B = \{1, 2, 3, 5\}$ A non-Venn diagram solution will be given, and the appropriate setting for my solution will be discussed

• Refuting a Conjecture On  $x^n - 1$  Using a Computer Algebra System, Michael Xue, Vroom Laboratory for Advanced Computing (SCIC 104)

A conjecture states that the absolute value of non-zero coefficient in the factor of  $x^n - 1$  is always 1. This presentation refutes this conjecture by a counter example using a computer algebra system (CAS). Furthermore, this talk will pose a similar problem to either prove or refute another conjecture regarding the uniqueness of a solution found by CAS

• Addressing Conservative Issues Associated with Adaptive Simulations, Godfred Yamoah, *Trine University* (SCIC 202) Adaptive simulation problems are often characterized by rapid changes in certain regions of the domain. Spatial adaption involves refining and coarsening the spatial mesh grid based on error estimates. However, significant mass-conservation errors can may occur if care is not taken during the coarsening phase of the adaption process. In the case where two elements or cells are merged in particular, nodal information must be re-distributed to preserve mass in the newly merged element. For this work we propose another scheme to preserve mass during the coarsening process and provide results on a one dimensional infiltration problem that has been well studied in the literature. The method seeks to redistribute mass on coarsened elements using solution values from the previous time step. Collaborators: Dr. Kathleen Fowler (Clarkson University, Potsdam NY)

# 1:35pm-2:25pm

- Math and Marriage Don't Call a Lawyer Yet, Ron Gould, Department of Mathematics, *Emory University* (SCIC 203) Beginning with Philip Hall's famed "Marriage" Theorem in 1935, the study of marriages (or matchings) has seen significant development, both theoretical and algorithmic. Taking a graph theoretic point of view, we will consider a number of *marriage* questions including:
  - 1. When can a set of *k* marriages be found?
  - 2. When we do find a set of *k* marriages, are there ways to optimize the pairings? Here we consider the famed stable marriage theorem.
  - 3. What ways are there to generalize the idea of marriage? The roommate problem and multi-matchings will be considered.
  - 4. What can we say about these generalizations? Is there an optimum form of marriage?

# 2:45pm-3:45pm

• **Proposal Writing Workshop**, Gene Fiorini, Department of Mathematics, *Muhlenberg College* (SCIC 203) Gene Fiorini will lead a brief workshop on proposal writing.

# **Alphabetical Listing of Talks**

**Antwi-Fordjour**, Global Dynamics of the Shadow Gierer-Meinhardt System with Mixed Boundary Conditions, 10:45am-11:10am, SCIC 104 **Barrios\***, Exceptional Elliptic Curves with Specified Torsion Subgroups, 11:20am-11:45am, SCIC 204

Collins, Aero Cube S4 Group Theory Blocks, 11:20am-11:45am, SCIC 202

Fiorini, Challenges of Researching Integer Sequences Using the OEIS, 9:40am-10:30am, SCIC 203

Fiorini, Proposal Writing Workshop, 2:45pm-3:45pm, SCIC 203

Fonstad, Implementing the 2015 CUPM Content Recommendations, 11:20am-12:20pm, SCIC 203

Gould, Math and Marriage - Don't Call a Lawyer Yet, 1:35pm-2:25pm, SCIC 203

Gould, Some Unusual Applications of Mathematics, 8:40am-9:30am, SCIC 203

Hoehn, Ethical Considerations in the Era of Big Data, 10:45am-11:10am, SCIC 204

Hummel, Implementing the 2015 CUPM Content Recommendations, 11:20am-12:20pm, SCIC 203

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Kim, Solutions of the nonlinear polyharmonic equation with periodic potential, 10:45am-11:10pm, SCIC 202

Lamichhane\*\*, Multilinear Algebra and its Applications, 11:20am-11:45am, SCIC 104

Lynch, Set Problems Involving Symmetric Difference, 11:55am-12:20pm, SCIC 101

Ma, Serious Math for Playful Young Minds, 11:20am-11:45am, SCIC 101

Morley\*\*, Results on Regular and Nearly Regular VE- and EV-Degree Sequences, 10:45am-11:10am, SCIC 101

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**Xue**, Refuting a Conjecture On  $x^n - 1$  Using a Computer Algebra System, 11:55am-12:20pm, SCIC 104

Yamoah, Addressing Conservative Issues Associated with Adaptive Simulations, 11:55am-12:20pm, SCIC 104